# Discussion of "Option Returns: A Tale of Two Expiration Rollover Days" by Garcia-Ares and Muravyev

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2025 Conference on Derivatives and Volatility

### Summary

- Daily-delta-hedged call option returns are
  - 0.19% from end of month to expiration—1
  - -0.43% from expiration-1 to expiration+2
  - 0.04% over rest of month
- Application: 18 option return anomalies can be mostly attributed to rollover days
- Explanation: demand pressure and intermediary frictions
  - As opposed to "generic market inefficiency or behavioral biases"

# Methodology

- Enter into option (> 1 month to expiration) at end of month, close at end of following month
- Compute monthly profit

$$\Pi_{t+\tau} = C_{t+\tau} - C_t - \sum_{n=0}^{N-1} \Delta_{C,t_n} \left[ S\left(t_{n+1}\right) - S\left(t_{n}\right) \right] - \sum_{n=0}^{N-1} \frac{a_n r_{t_n}}{365} \left[ C\left(t_n\right) - \Delta_{C,t_n} S\left(t_n\right) \right]$$

- Return = profit scaled by the absolute value of the initial investment  $(|\Delta_t S_t C_t|)$
- Decompose monthly return into expiration/rollover days and other days
  - Not equivalent to separately computing rollover return and non-rollover return

$$\frac{P_c}{P_{c-1}} - 1 = \frac{P_o}{P_{c-1}} \times \frac{P_c}{P_o} - 1 = \frac{P_o - P_{c-1}}{P_{c-1}} + \frac{P_c - P_o}{P_{c-1}}$$

## Methodology: adjust the delta hedge daily

- Daily delta hedging matters: for 8/13 overlap anomalies, average delta-hedged return is statistically insignificant in Duarte et al (2025)
- Hence, 1) "resurrect" anomalies, 2) explain them
- For completeness, the paper should report everything with one-time delta hedging (Table A1 is not for anomalies)
- Magnitudes seem larger with one-time delta hedging (Table A1), however
  - "Daily delta hedging does not affect average returns, but greatly decreases their volatility" (p.6)
- This could affect the interpretation: why do intermediary frictions imply stronger/weaker daily-delta hedged anomaly return?

# Anomaly returns

	Daily Delta-Hedged Monthly Call Option Returns					urns
	Full Month Ex-rollover			Rollover		
	D1	D10	D10-D1	D1	D10	D10-D1
AVERAGE ANOMALIES	0.46 (4.87)	0.18 (1.33)	-0.28 (-3.90)	-0.29 (-13.20)	-0.66 (-16.51)	-0.36 (-13.69)
CFV	0.50	0.24	-0.25	-0.27	-0.56	-0.29
C1 *	(4.78)	(1.76)	(-2.34)	(-11.79)	(-14.68)	(-9.37)
CH	0.54	0.09	-0.46	-0.28	-0.70	-0.42
	(4.96)	(0.63)	(-4.20)	(-9.93)	(-17.95)	(-13.27)
DISP	0.41	0.46	0.04	-0.25	-0.54	-0.28
	(4.47)	(3.67)	(0.70)	(-10.78)	(-14.56)	(-11.01)
$ISSUE_1Y$	0.41	0.29	-0.12	-0.28	-0.60	-0.33
	(4.19)	(2.21)	(-1.63)	(-11.19)	(-15,36)	(-10.12)
$ISSUE_{\pi}Y$	0.45	0.16	-0.29	-0.26	-0.55	-0.30
	(4.57)	(1.22)	(-4.10)	(-11.48)	(-13.48)	(-8.57)
-PM	0.51	0.11	-0.40	-0.38	-0.74	-0.35
	(4.70)	(0.74)	(-4.46)	(-12.87)	(-17.96)	(-9.68)
-Ln(PRICE)	0.36	0.21	-0.15	-0.22	-0.78	-0.56
()	(3.51)	(1.24)	(-1.07)	(-9.74)	(-14.82)	(-11.35)
PROFIT	0.37	0.35	-0.02	-0.34	-0.57	-0.24
	(3.54)	(2.86)	(-0.27)	(-12.42)	(-14.99)	(-9.40)
TEF	0.43	0.27	-0.16	-0.30	-0.69	-0.39
	(4.88)	(1.90)	(-1.68)	(-12.34)	(-14.72)	(-9.51)
ZS	0.31	0.21	-0.10	-0.56	-0.64	-0.08
	(2.32)	(1.37)	(-0.76)	(-13.34)	(-13.92)	(-1.76)
VOL DEVIATION	0.95	-0.55	-1.51	-0.38	-0.64	-0.25
	(6.96)	(-3.63)	(-8.92)	(-12.45)	(-14.32)	(-7.20)
IVOL	0.35	0.15	-0.21	-0.19	-0.75	-0.57
	(4.48)	(0.96)	(-1.92)	(-9.04)	(-16.75)	(-15.35)
Ln(AMIHUD)	0.33	0.55	0.22	-0.26	-0.57	-0.31
` '	(3.31)	(3.23)	(1.40)	(-10.84)	(-11.18)	(-6.49)
Ln(ME)	0.33	0.37	0.04	-0.24	-0.64	-0.40
	(3.48)	(2.18)	(0.24)	(-10.24)	(-11.71)	(-7.83)
MF SKEW	0.62	0.54	-0.09	-0.24	-0.48	-0.24
	(6.35)	(3.87)	(-1.13)	(-9.45)	(-10.65)	(-6.54)
CALL IV ATM	0.50	-0.47	-0.98	-0.14	-1.01	-0.87
	(5.79)	(-2.66)	(-6.37)	(-7.54)	(-18.08)	(-17.13)
-IV TERM	0.52	0.05	-0.47	-0.49	-0.72	-0.22
	(4.58)	(0.33)	(-4.46)	(-14.92)	(-13.71)	(-5.93)
MAX(1)	0.35	0.25	-0.11	-0.21	-0.66	-0.44
	(3.86)	(1.69)	(-1.10)	(-9.50)	(-16.74)	(-14.33)

Negative returns for all portfolios on rollover days

# Anomaly returns

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Positive returns for all but two portfolios on ex-rollover days

#### Anomaly returns: interpretation

- The long-short spread becomes more extreme (per day) around rollover days
- This is unlike many "seasonality patterns" in stock returns where the spread switches sign
  - January vs other months (Keloharju, Linnainmaa, and Nyberg, 2016; Bogousslavsky, 2015)
  - Day of the week (Birru, 2018)
  - Day and night (Lou, Polk, and Skouras, 2019)
  - Intraday intervals (Bogousslavsky, 2021)
- An "amplified" spread seems consistent with intermediary frictions (perhaps less so with behavioral explanations based on mood or other clientele effects)

## Do we see anything for stock return anomalies?

	average anomaly daily return (bps)				
	Baseline	DoW	DoW + 3rd Friday/Monday		
constant	1.73**				
	(0.84)				
Monday		6.82***	6.97***		
		(2.17)	(2.39)		
Tuesday		2.23	2.23		
		(1.92)	(1.92)		
Wednesday		0.79	0.79		
		(1.88)	(1.88)		
Thursday		0.77	0.77		
		(1.82)	(1.82)		
Friday		-1.63	-3.23*		
		(1.58)	(1.84)		
3rd_friday			6.84*		
			(3.53)		
opex_monday			-0.66		
			(5.56)		

Sample: 1996-2024; 'Cash\_ret', 'Sharelss1Y\_ret', 'Sharelss5Y\_ret', 'VarCF\_ret', 'ForecastDispersion\_ret', 'Price\_ret', 'OperProf\_ret', 'IdioVol3F\_ret', 'Illiquidity\_ret', 'RealizedVol\_ret', 'MaxRet\_ret' from open source asset pricing library (Chen and Zimmermann, 2022)

⇒ suggestive of an option-specific explanation

### Smoking gun: order imbalance

Figure 3. Option Order Imbalances around the standard monthly expiration day

0.06

0.04

0.02

0.04

0.05

0.08

0.11

0.12

0.14

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0.15

- Imbalance persistently negative, but no effect on  $r_{t+2}$ 
  - Price impact of anticipated imbalance should be lower
  - Nonlinear return-imbalance relation (Table 3)
- In standard inventory model, reversal compensates liquidity providers, but there is no reversal here
  - More discussion from the perspective of the market maker would help

### Additional suggestions

- How related are the option anomalies? Show the correlation matrix on all days, rollover days, and other days
- For a trader, would it make sense to roll the position earlier to incur less price impact?
  - Is the traders' behavior "rational" given the pattern?

### In summary

- Nice paper with a striking finding!
- The intermediary friction explanation is intuitive
- It would help to dig deeper into the order imbalance evidence and the prediction of inventory models
- Good luck!